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# Performance Prediction for Distributed Load Balancing in Multicomputer Systems

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Load Balancing in Multicomputer Systems***

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April 1991

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# Abstract

Computing literature has been flooded recently with a plethora of dynamic load balancing strategies for multicomputer systems. The diversity of many strategies and their dependence on a number of parameters has made it difficult to compare their effectiveness on a unified basis. Not only does each strategy consider a different environment, but the simplified assumptions obscure the relative merits and demerits of each strategy. This paper presents a solution to compare different load balancing schemes on a unified basis. Our approach, which is an integration of simulation, statistical and analytical experiments, takes into account the fundamental system parameters that can possibly affect the performance. We show that a class of distributed load balancing strategies can be modeled by a central server open queueing network. Furthermore, these load balancing strategies can be characterized by only two queueing parameters – the average execution queue length and the probability that a newly arrived task is to be executed locally or migrated to another node. To capture the relation between these queueing parameters and various system parameters, a statistical analysis has been carried out on the empirical data obtained through simulation. The analytical queueing model is then used to predict the response time of a system with any set of system parameters. Experimental results are obtained for seven different load balancing strategies. The proposed model directly provides performance results in a straight forward manner and can be beneficial to the system designers in order to assess the system under varying conditions.

## 1. Introduction

Efficient utilization of a multicomputer system lies in its ability to efficiently partition and balance computational load among its computing nodes. With the increasing popularity of multicomputer systems, researchers and system designers have been focusing on these essential issues. There is a clear distinction between dynamic load balancing, also known as load sharing [5] or load distribution [10], and static load balancing [3]. In the former case, work load allocation decisions are taken at run time rather than at compile time. As noted in [5], any simple dynamic load balancing algorithm improves the performance of the system, and is better than no load balancing. Dynamic Load balancing strategies are characterized by the manner in which information exchange and control of work load allocation takes place. The control can be centralized [16], fully distributed [2], [4], [5], [6], [11], [14], [17], [24] or

semi-distributed [1]. With fully distributed control, the load balancing strategy is incorporated at every node of the system in that each node in the system makes autonomous decisions. A node is subject to arrival of tasks, locally generated or migrated from some other node. The node decides whether the new task should be executed locally or it should be transported to some other node. If the task is decided to be migrated, the local node needs to know the load status of other nodes. Once the state information about other nodes is received, the target node can be selected in a number of ways. A node for task migration can be selected randomly [5], [8], [24] or it can be selected if it has the lowest load [5]. However, the accuracy of scheduling decisions in a decentralized algorithms, depends on the accuracy and amount of state information [10]. Intuitively, getting more information should result in a more accurate decision-making. Although decentralized models have potential advantages over centralized models, they can incur large overhead due to information exchange and task migration [6].

Wang and Morris [25] proposed a number of relatively simple load balancing algorithms and classified them into two categories : source-initiated and server-initiated. In a source-initiated algorithm, tasks enter the distributed system via source nodes and are processed by server nodes. A demand driven model, using a gradient plane, was suggested by Lin and Keller where lightly loaded processors initiate request for load [13]. Fox *et al.* [7] presented a load balancing scheme by making use of the analogy of load balancing to minimizing an appropriate energy function. In [17] and [22], various bidding algorithms have been proposed which belong to the sender-initiated class. A drafting algorithm belongs to the server-initiated class [15]. A comparison of these two types of algorithms [18] reveals that in spite of the fact that the bidding algorithm suffers from *task-dumping* or *task-thrashing*, it performs consistently better than the drafting algorithm. Task-thrashing is a phenomenon associated with load balancing schemes where a lightly loaded node can become a victim of task arrivals from other nodes [8], [14]. Load balancing algorithms can also suffer from *state wobbling* – another performance decaying phenomenon in which processors frequently change their status between low and high [18].

Distributed load balancing schemes based on task migration among nearest neighbors have gained considerable attention. In a number of independent studies [8], [10], [12], [19], variants of this strategy have been proposed and their effectiveness has been proven both by simulation and implementation observations. Kalé [19] have compared one version of this strategy, known as Contracting Within Neighborhood (CWN), to Gradient Model [13] and

have shown that CWN spreads the load more quickly and performs better. In two more studies [8], [19], the concept of load averaging among neighbors is introduced. The advantage of load averaging is that each node tries to keep its own load equal to the average load among its nearest neighbors. Shu and Kalé [21] have proposed and implemented a revised version of CWN known as Adaptive Contracting Within Neighborhood (ACWN) which consistently shows better response time compared to the Gradient model and Random strategy. Grunwald *et al.* [10] have proposed a classification scheme for the type of information required to make load balancing decisions. For large-scale multicomputer systems consisting of hundreds or thousands of nodes, a semi distributed strategy was proposed in [1]. The semi distributed strategy combines the advantages of centralized and fully distributed load balancing strategies by partitioning the system into independent spheres and load balancing is performed by only a selected set of nodes.

Given the diversity of a number of proposed strategies and their dependence on a number of parameters, it is difficult to compare their effectiveness on a unified basis. One particular strategy may perform well under a certain combination of parameters such as system load or system communication rate on a certain topology. The same strategy may be outperformed by another strategy due to difference in information collection and scheduling overhead. In addition, simplified assumptions and neglecting important parameters sometimes obscures the relative merits and demerits of each strategy. This paper presents an approach to predict and compare different load balancing schemes based on a unified basis. Our approach, which is an integration of simulation, statistics and analytical models, takes into account various system parameters, such as system load, task migration time, scheduling overhead and system topology etc., that can possibly affect the performance. We show that a class of load balancing strategies can be modeled by a central server queuing network. We also show that these load balancing strategies can be characterized by only two parameters – the average queue length and the probability that a newly arrived task is to be executed locally or migrated to another node. Through an extensive simulation, a large number of values of the average queue length and the probability associated with task migration have been obtained. A statistical analysis has been performed on these data points to capture the relation between the queueing parameters and the system parameters. We then use the analytical queuing model to predict the response time of a system with any set of parameters. Seven different load balancing algorithms have been studied and characterized.

This performance prediction approach has many advantages. First, instead of assessing a particular strategy on the basis of a selected set of experiments, any combination of parameters can be used to predict the performance. Second, all strategies can be relatively compared by selecting more appropriate and realistic parameters. Finally, an existing system can be tuned, and a system design can be evaluated before it is actually built. The response time predicted by the model is compared with the response time produced by simulation for all eight strategies.

## 2. Selected Load Balancing Strategies

We consider a fully homogeneous multicomputer system in which processing nodes are connected with each other through a symmetric topology, that is, each node is linked to the same number of nodes. The number of links per node, called the degree of the network, is considered as one of the system parameters and is denoted as  $L$ . The work load submitted to the system is assumed to be in the form of tasks, which are submitted to each node with an average arrival rate of  $\lambda$  tasks per time-unit per node. The task arrival process is assumed to be Poisson. The load balancing control is fully distributed for which each node makes an autonomous decision to schedule a task by collecting the load status information from its neighbors. A task is either scheduled to a local execution queue or it is migrated to one of the neighbors connected with each communication channel. Seven different load balancing strategies have been chosen which are fully distributed but differ in information collection and scheduling policies. The information and scheduling takes a certain amount of time, which is assumed to be exponentially distributed with an average of  $1/\mu_s$  time-units. Information is collected by a hardware/software component at each node and is called Collector/Scheduler.

Since information interchange and execution of scheduling algorithm takes certain amount of time, the tasks arriving during that time wait in a waiting queue. For each communication link, a communication queue is maintained. The underlying network supports point-to-point communication and the communication channel is model by a server. A communication server transfers a task from one node to another with an average of  $1/\mu_c$  time-units. The task communication time is also assumed to be exponentially distributed and all network links are assumed to be identical. At each node, the incoming traffic from other nodes joins the locally generated traffic, and both are handled with equal priority. Each node maintains an execution queue in which locally scheduled tasks are served by a CPU on the

FCFS basis . A task may migrate from node to node in the network before finally being executed at some node. The execution time is also assumed to be exponentially distributed with an average of  $1/\mu_E$  time-units.

We have analyzed seven different load balancing strategies for varying information collection mechanisms and scheduling disciplines. The selected strategies belong to the sender-initiated class. Based on the information interchange mechanism, these strategies can be further classified into two categories. In the first category, the information about load and status of other nodes is collected at the time a task is scheduled for execution or migration. The load is expressed in terms of the length of the execution queue. This load metric has been widely accepted and experimental results have shown that it accurately reflects the CPU load [18]. In the second category, nodes exchange the load information among their neighbors periodically. Within each category, we have considered three different scheduling policies. In addition, one more strategy is proposed which uses a different scheduling policy but requires non-periodic information. The seven strategies are described below.

### **Category I: Information Exchange at the Time of Task Schedule**

- **FRandom:**

In this strategy, the task scheduler calculates the average of the local load and the load of all neighbors. If the local load is greater than the average, the task is sent to a randomly selected neighbor. If some tasks are already waiting in the communication queue for that neighbor, the task joins that queue. Each communication queue is served on the FCFS basis. If the local execution queue is empty (or local load is less than the average), then the task is sent to the local execution queue.

- **FMin:**

In this strategy, the task scheduler sends a new task to the node which has the minimum load. However, if the local node's load is equal to the minimum load among neighbors, the local node is given priority.

- **FAverage:**

In this strategy, the task scheduler calculates the average of all neighbors' load and its own load. If the local load is greater than the average, the task is sent to the neighbor with the minimum load. However, if the local execution queue is empty or local load is less than the average, then the task is sent to the local execution queue.



## **Category II: Information Exchange with Periodic Interval**

- **PRandom:**

This strategy is similar to *FRandom* except that every node sends its own load information to all its neighbors periodically. The time period,  $T_u$  for sending messages is a system parameter.

- **PMin:**

This strategy is similar to *FMin* except that information exchange is done periodically.

- **PAverage:**

This strategy is similar to *FAverage* except that information exchange is done periodically.

In addition to the above mentioned six strategies, a new strategy, *Bidd-Average*, is proposed and analyzed. This strategy is described below.

- **Bidd-Average:**

This strategy is a combination of neighborhood averaging and bidding approach. When a task is to be scheduled, the scheduler broadcasts messages to its neighbors asking for bids. A neighbor calculates the average load of its own neighborhood and if its own load is less than that average, it sends a *yes* message along with its load information to the requesting node. After the requesting node has received all the bids, it calculates the average load of its neighborhood. If its local load is greater than average, it selects the node with minimum load out of those neighbors which sent *yes* messages. If the local execution queue is empty or the local load is less than average and none of the neighbors reply with *yes* messages, the task is scheduled in the local queue. This strategy is proposed to add more stability to neighborhood averaging strategy. This extra level of stability is due to the fact that the receiving node expresses its willingness to receive a task only if its load is less than its own neighborhood average.

## **3. The Performance Prediction Model**

In this section, we describe a performance prediction model for distributed load balancing strategies described above. The model is an integration of simulation, and statistical and queuing models. First, we describe the queuing model and show that the class of distributed load balancing strategies described above can be modeled by an open central server queuing model.

### 3.1. The Queuing Model

As described above, the multicomputer system considered here is symmetric and homogeneous. By symmetry, we mean that the interconnection network of the system is a regular graph with fixed number of links per node. By homogeneity we imply that the processors of the system have identical processing speeds. Similarly all communication channels and task schedulers are identical. With nearest neighbor load balancing, the steady state departure and task arrival rates at a node are the same. As explained earlier, a task keeps on migrating until it finds a suitable node. When a task migrates from one node to another, it sees a statistically identical node. Therefore, the steady-state behavior of nearest neighbor load balancing can be approximated by the open central server queuing model as shown in Figure 1. The model consists of a waiting queue,  $L$  communication queue sand an execution queue. The model is approximate since routing of tasks is dependent on the state of execution queues. However, as described in next section, simulation results obtained on actual network

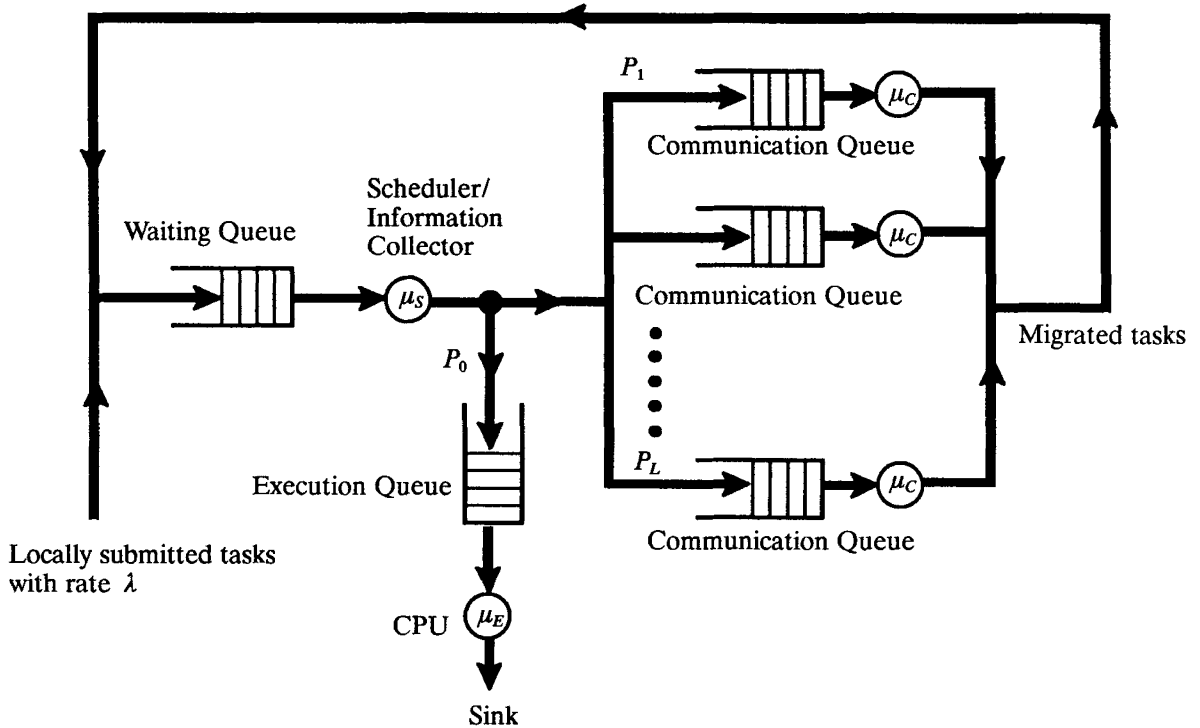


Figure 1: Distributed load balancing represented by open central server model

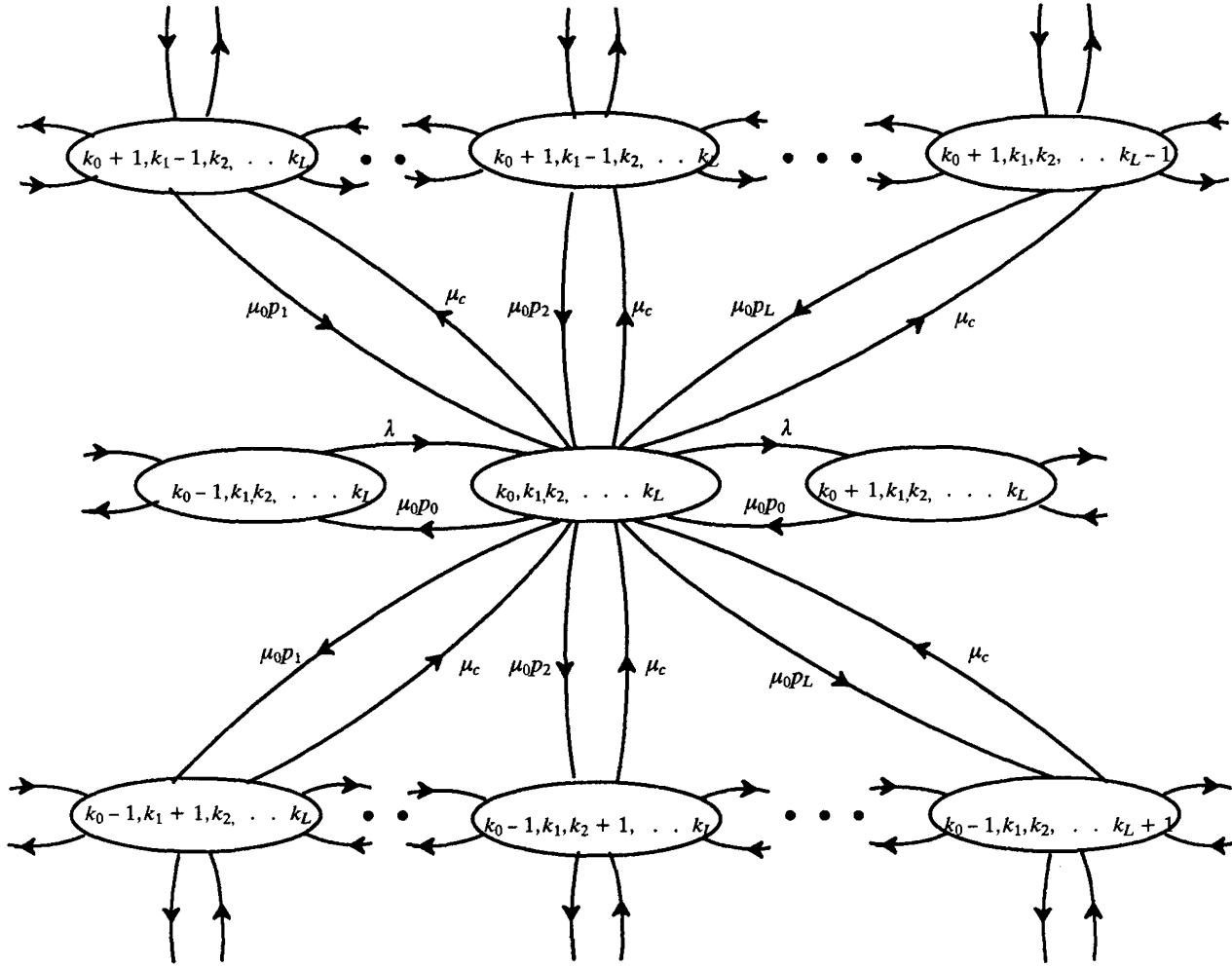


Figure 2: Markov chain with state of the chain describing number of tasks at each queue of a node

topologies are very close to the analytical results determined from this model which validate that the proposed model of Figure 1 indeed represents the task scheduling and migration process.

A task's residence time in the system can be viewed as consisting of two phases. In the first phase, the task may keep on migrating during the course of which it waits in the waiting queue, gets service from the scheduler, waits in the communication queue, and then transfers to another node. At that point the same cycle may start all over again. Once the task is scheduled at the execution queue of a node, the second phase starts which includes the queuing and service time at the CPU. In the first phase, the task can be viewed as occupying either the task

scheduler or one of the communication links. The Markov chain model shown in Figure 2 describes the behavior of the central server which in turn explains the task migration phenomenon before the task enters the execution queue. The state of the Markov chain is described by  $(L + 1)$  tuple,  $k_0, k_1, \dots, k_L$  in which  $k_i$  represents the number of tasks at the  $i$ -th queue ( $0 \leq i \leq L$ ) at a node.

It follows [23] that the model can be solved by the Jacksonian network which has the product form solution; that is, the joint probability of  $k_j$  tasks at queue  $j$  ( $j = 0, 1, \dots, L$ ) is given by the product :

$$p(k_0, k_1, \dots, k_L) = \prod_{j=0}^L p_j(k_j).$$

where  $p_j(k_j)$  is the probability of  $k_j$  tasks at  $j$ -th queue and is given by:

$$p_j(k_j) = (1 - p_j) p_j^{k_j}.$$

It implies that the lengths of all queues are mutually independent in a steady-state. The above model can also be solved if considering the probabilistic behavior of a task. Suppose, after the task is served by the scheduler, it goes to the  $i$ -th link with probability  $P_i$  or it enters the local execution queue with the probability  $P_0$ . When a task leaves (enters) the waiting queue, the number of tasks in that queue is decreased (increased) by one. Similarly, when a task is served by the communication, a statistically identical task joins the waiting queue. For the  $j$ -th component, the average utilization,  $Q_j$ , is equal to  $\lambda_j/\mu_j$  and the average queue length and the average response time are given by

$$E[N_j] = \frac{Q_j}{1 - Q_j} \quad \text{and} \quad E[R_j] = \frac{1}{\lambda} \frac{Q_j}{1 - Q_j}.$$

respectively.

The average number of tasks at a node is the sum of the average number of tasks at each component of a node and is given by:

$$E[N] = \sum_{j=0}^L E[N_j] = \sum_{j=0}^L \frac{Q_j}{1 - Q_j}.$$

from which the average response time before the task is scheduled in the execution queue can

be computed as [23]:

$$\begin{aligned}
E[R_S] &= \frac{1}{\lambda} \sum_{j=0}^L \frac{q_j}{1 - q_j} \\
&= \frac{1/(P_0\mu_0)}{1 - \lambda/(P_0\mu_0)} + \sum_{j=1}^L \frac{p_j/(P_0\mu_j)}{1 - \lambda p_j/(\mu_j P_0)} .
\end{aligned}$$

Once a task is scheduled at a local execution queue, the response time from the time it is scheduled to the time it finishes execution is given by

$$E[R_E] = \frac{E[N_E]}{\lambda} .$$

where  $E[N_E]$  is the average execution queue length. The complete response time, therefore, is given by

$$E[R] = E[R_S] + E[R_E] .$$

The above equation implies that, for a given system load,  $\mu_0$  and  $\mu_j$ 's, the response time yielded by a load balancing strategy can be calculated if the probability,  $P_0$ , and the average execution queue length,  $E[N_E]$  is determined. In other words,  $P_0$ , is the probability with which a load balancing strategy schedules the tasks locally. The probability that a task will be migrated to another node is simply  $1 - P_0$  and migration probabilities to individual channels at each node are identical. The average execution queue length,  $E[N_E]$ , determines how smoothly load is balanced. Both parameters,  $P_0$  and  $E[N_E]$ , depend on system parameters such as  $\lambda$ ,  $\mu_S$ ,  $\mu_C$ ,  $\mu_E$ , and  $L$ . In the next sections, we briefly describe the simulation methodology which was used to obtain a very large data set from different test cases. We describe how we performed statistical analysis on the simulation data and determined the sensitivity of  $P_0$  and  $E[N_E]$  against different system parameters

## 3.2. The Simulation Model

The above mentioned load balancing strategies were simulated on an Encore Multi-max. The simulator accepts the topology of the network along with  $\lambda$ ,  $\mu_S$ ,  $\mu_C$ ,  $\mu_E$ , length of simulation run, and choice of load balancing strategies and their associated parameters. The results produced by the simulator include average response time, utilization of individual

nodes, average time spent in communication, average number of messages, throughput, average number of migrations made by a task and their distribution, average lengths of waiting, communication and execution queues. In addition to average values, the variance and each node's individual statistics are also produced. The average number of tasks transferred and received at each node are also recorded. The probability,  $P_0$ , is then calculated by dividing the average number of locally scheduled tasks by the total number of tasks arrived, at each node. The important aspects of discrete-event simulation are that it should be run for sufficiently long time and initial transients should be removed before starting the accumulation of statistics. Moreover, the confidence interval must be calculated after running the same experiment with multiple independent streams. All of these features have been incorporated in the simulator and all results are obtained with a 99 % confidence interval.

A long series of simulation runs was conducted to obtain a large number of data points for  $P_0$  and  $E[N_E]$  for each particular strategy. Three different topologies were selected which included the ring, the hypercube and the folded hypercube [9], each consisting of 16 nodes. Each point for one particular strategy was obtained on each of the topologies by fixing one parameter and varying the rest. In most cases,  $\lambda$  was varied from 0.3 to 0.9 tasks per time-unit,  $\mu_S$  was varied from 8 to 16 tasks per time-unit and  $\mu_C$  was varied from 8 to 16 task per time-unit. The task execution rate,  $\mu_E$ , was fixed as 1 task per time-unit in all cases. For strategies that required a periodic information update, the update time,  $T_u$ , period was varied from 0.5 time-units to 1.5 time-units. A total of 3500 data values for  $P_0$  and  $E[N_E]$  were obtained.

It is worth mentioning that the simulator takes into account the time to schedule a task which includes the exchange of state information and the execution of scheduling algorithm itself. Most previous studies have ignored this overhead. We have assumed an average scheduling time,  $1/\mu_S$ , which in turn can be normalized with respect to the execution time,  $\mu_E$ . In other words, when  $\mu_S$  is 10 tasks/time-unit and  $\mu_E$  is 1 task/time-unit, it means that the average task scheduling time is 1/10 of the execution time. We consider it an input parameter which can be observed from a real system depending upon how the information message handling and regular task migration is implemented.

### 3.3. Statistical Analysis

In order to characterize  $P_0$  and  $E[N_E]$  in terms of system parameters such as  $\lambda$ ,  $\mu_S$ ,  $\mu_C$ ,  $T_u$  and system network topology, statistical analyses have been performed. As described above, data on  $P_0$  was collected for various values of the system parameters, for each load balancing strategy. A regression analysis was then performed to obtain a model that expresses  $P_0$  in terms of the aforementioned parameters. It is observed that the following model works quite well for all seven strategies.

$$P_0 = \left[ 1 + e^{-\left( \alpha_p + \beta_{1p}links + \beta_{2p}\mu_C + \beta_{3p}\mu_S + \beta_{4p}\lambda + \beta_{5p}T_u \right)} \right]^{-1}$$

The estimates of  $\alpha_p$  and coefficients,  $\beta$ 's, are given in Table I along with measures that describe how good the above model predicts the observed  $P_0$ . For instant, in case of FRandom, R-Square value is 0.9277 which implies that the regression model is able to compute 92.77 % of variation observed values of  $P_0$ .

A similar regression analysis approach is taken to characterize  $E[N_E]$  in terms of system parameters. In this case, the observed model is:

$$E[N_E] = \exp \left( \alpha_q + \beta_{1q}links + \beta_{2q}\mu_C + \beta_{3q}\mu_S + \beta_{4q}\lambda + \beta_{5q}T_u \right)$$

This model fits extremely well as is observed from its R-Square values ( all R-Square values are 99 %) given in Table II. In case of  $E[N_E]$ , the coefficients for  $\mu_S$  and  $\mu_C$  were found insignificant and hence are ignored.

### 3.4. The Complete Model

The complete model for performance prediction is shown in Figure 3. The performance measure is the average task response time. As described above, the model building consisted of running a large number of simulations and then applying statistical analysis to obtain models for  $P_0$  and  $E[N_E]$ . Using these model, the values of  $P_0$  and  $E[N_E]$  can be directly computed for any of the seven load balancing with any combination of system load, communication rate, task scheduling rate, load update period (for load balancing strategies belonging

Table I: Estimation for  $P_0$  and its sensitivity versus system parameters

Strategy	R-Square	System Parameter	Coefficient Estimate
FRandom	0.9277	$\alpha$	1.72220
		<i>Links</i>	-0.15421
		$\mu_C$	0.00116 †
		$\mu_S$	0.00140 †
		$\lambda$	-1.32043
FMin	0.9505	$\alpha$	3.39618
		<i>Links</i>	-0.02139
		$\mu_C$	0.00881
		$\mu_S$	0.00841
		$\lambda$	-3.02439
FAverage	0.8668	$\alpha$	1.48038
		<i>Links</i>	-0.09421
		$\mu_C$	0.00839
		$\mu_S$	0.01214
		$\lambda$	-1.04726
PPandom	0.9356	$\alpha$	1.63440
		$T_U$	-0.13364
		<i>Links</i>	-0.13337
		$\mu_C$	-0.00214 †
		$\mu_S$	-0.00395
PMin	0.9683	$\alpha$	-1.23230
		$T_U$	4.06852
		<i>Links</i>	-0.21302
		$\mu_C$	-0.10590
		$\mu_S$	0.00013 †
PAverage	0.9038	$\lambda$	0.00300
		$\alpha$	-3.48994
		$T_U$	2.16996
		<i>Links</i>	-0.42800
		$\mu_C$	-0.14715
Bidding-Average	0.9103	$\mu_C$	-0.00146 †
		$\mu_S$	-0.00356
		$\lambda$	-1.46303
		$\alpha$	1.34904
		<i>Links</i>	-0.10827
		$\mu_C$	0.00559
		$\mu_S$	0.01331
		$\lambda$	-0.79433

Note: All estimates of model parameters are statistically significant except

† slightly significant

‡ not significant



Table II: Estimation for  $E[N_E]$  and its sensitivity versus system parameters

Strategy	R-Square	Parameter	Parameter Estimate
FRandom	0.9931	$\alpha$	-1.96055
		<i>Links</i>	-0.06211
		$\lambda$	3.30085
FMin	0.9926	$\alpha$	-1.67735
		<i>Links</i>	-0.03932
		$\lambda$	-2.86089
FAverage	0.9945	$\alpha$	-1.92121
		<i>Links</i>	-0.05420
		$\lambda$	3.07851
PRandom	0.9981	$\alpha$	-1.86021
		$T_U$	-0.02244
		<i>Links</i>	-0.05787
		$\lambda$	3.08250
PMin	0.9953	$\alpha$	-1.59469
		$T_U$	0.01106
		<i>Links</i>	-0.03587
		$\lambda$	2.70488
PAverage	0.9984	$\alpha$	-1.85252
		$T_U$	-0.00950
		<i>Links</i>	-0.05200
		$\lambda$	2.94949
Bidding-Average	0.9976	$\alpha$	-1.83433
		<i>Links</i>	-0.05526
		$\lambda$	2.91303

to category II) and network topology. We then compute the average response time by using the formula given in section 3.1.

As explained earlier, this response time consists of two parts. The first part is the average response time before a task is scheduled in an execution queue. This is simply equal to the time the task is scheduled (in the execution queue of some node) minus the task arrival time. This response time, called transient time, is completely described by  $P_0$  which indicates the task migration tendency of a load balancing strategy. The second part of average response time shows how much time (queueing delay plus execution time) a task takes after eventually being scheduled. This time is equal to the time the task finishes execution minus the time the task was scheduled in the execution queue. The best transient response time results when a strategy's  $P_0$  is neither very high nor very low. In other words, the strategy should not have

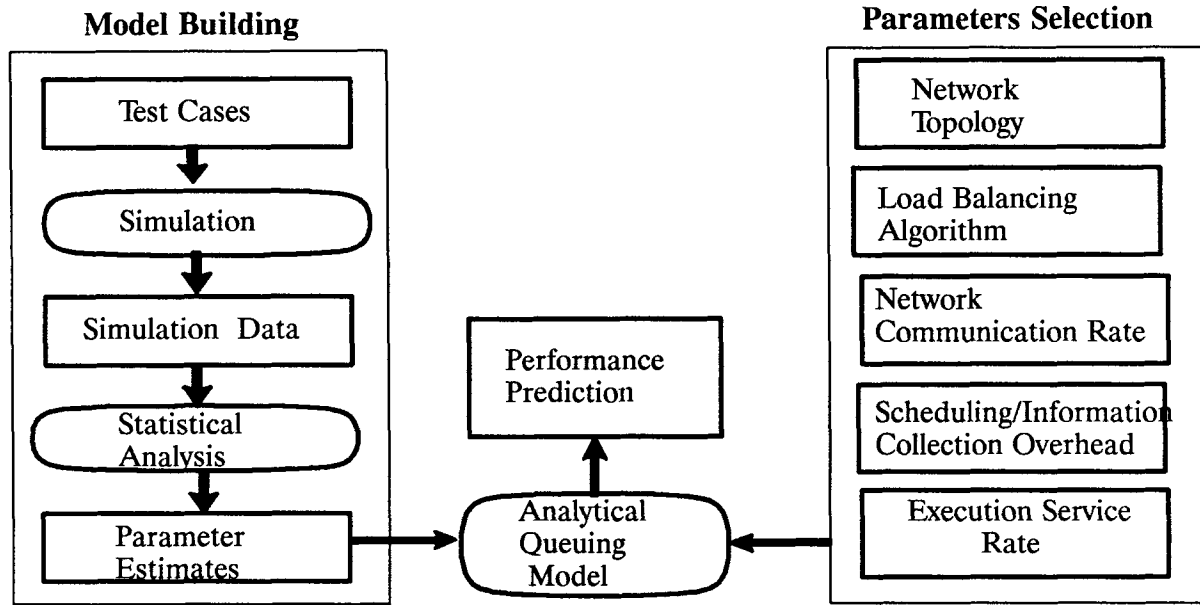


Figure 3: The complete Performance Prediction Model

task thrashing tendency and yet it should make task migrations whenever appropriate. The second part of the response time depends on a strategy's load equalization ability, that is, a smaller average execution queue length will result if load is equally balanced. Both factors, however, are dependent on each other. For example, if a strategy suffers from task thrashing, execution queue length is not balanced and the average value of queue length increases.

As an example, Figure 4 shows the plot of  $P_0$  versus system load for all seven strategies, on a 16 node hypercube. We notice that at low load both FMin and PMin have high values of  $P_0$  which sharply increase at high load. This implies that both Min strategies schedule more tasks locally (and hence make less migrations) but transfer more tasks at high load. In contrast, both 'random' strategies have low values of  $P_0$  which implies that greater task migration takes place using random algorithms. Figure 5 shows the variations in  $E[N_E]$  versus system load for all seven strategies. From this figure, we observe that, in this case, the value of  $E[N_E]$  is the minimum with *Bidd-Average*, followed by *FAverage* and *PAverage* and *PMin* results in the largest average queue length.

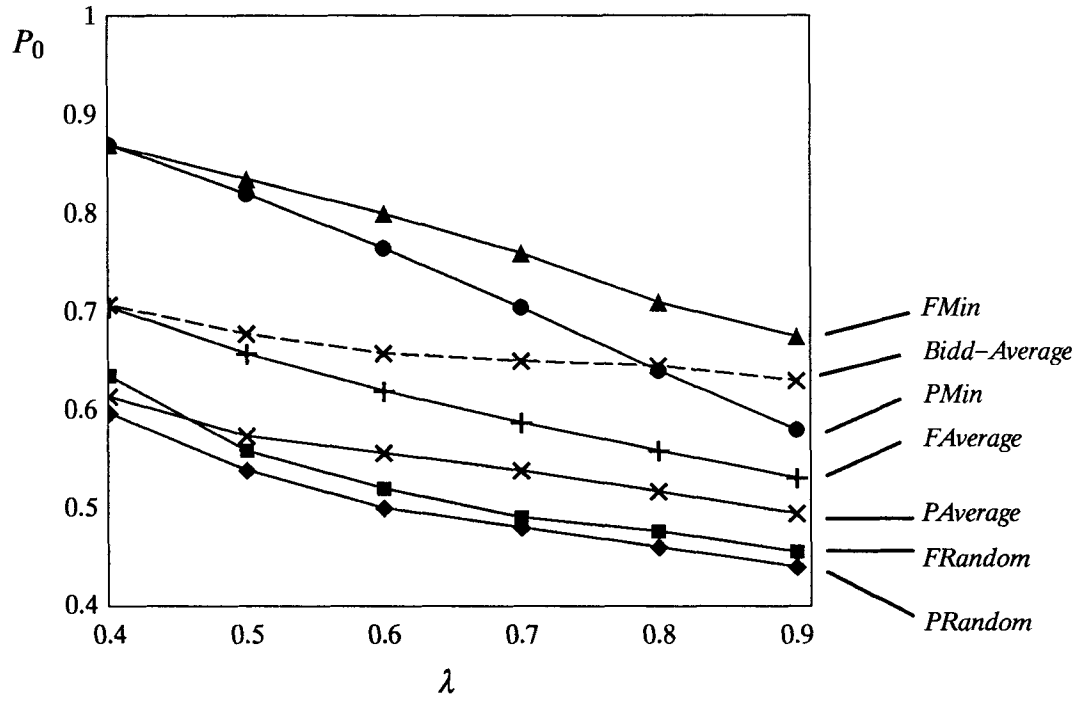


Figure 4: Variations in Probability  $P_0$  versus system load for various load balancing strategies

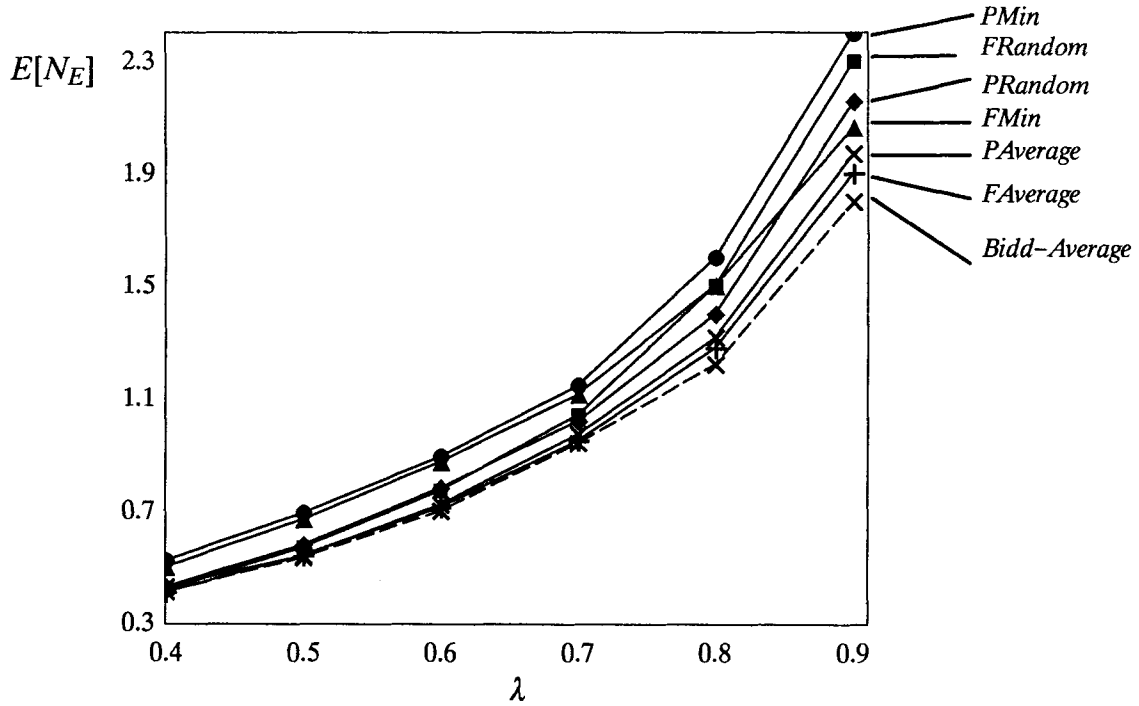


Figure 5: Variations in  $E[N_E]$  length versus system load for various load balancing strategies

## 4. Performance Prediction, Evaluation and Comparison

After obtaining response time data from the performance prediction model, we compare it with the observed simulation results. Seven load balancing strategies along with varying values of  $\lambda$ ,  $\mu_S$ ,  $\mu_C$ ,  $T_u$  and different network topologies provide a wide range of figures to make a comparison between the response time obtained with the model and the response time obtained with simulation. However, we compare the two figures by varying one parameter while keeping the rest constant. The results are quite encouraging and the difference between the two figures is found to be less than  $\pm 7\%$ . Since all results cannot be provided within the limited space of this paper, we present only those results with noticeable impact of each parameter on response time produced by the model as well as by the simulation.

First, we examine the impact of system load on the average response time for all seven strategies, shown in Figure 6 and Figure 7. In both figures, we have plotted the pairs of average response time computed from the model and the average response time observed from simulation. The task scheduling rate,  $\mu_S$ , and the task communication rate  $\mu_C$  are both 16 tasks/time-unit. System topology is a 16 node hypercube network and load update period,  $T_u$ , is 0.5 time-units. In Figure 6, system load  $\rho$  is 0.5 (with  $\lambda = 0.5$  and  $\mu_E = 1$ ). Figure 7 differs from Figure 6 in that the system load is increased from 0.5 to 0.7. From these figures, we observe the following.

- The difference in the response time computed from the model and the response time observed from simulation is very small. For most of the cases, this difference is less than 1%. The worst case difference is 6.52%.
- At low loading conditions, *Bidd-Average* and *FAverage* perform equally well whereas *PRandom* performs the worst of all. The difference in the performance of *FRandom* and *PRandom* is not significant which implies that for random algorithms, information exchange can be done either instantaneously or periodically with  $T_u = 0.5$ .
- The Difference in the performance of *FMin* and *PMin* is not significant. Again, this implies that information update can be done by selecting either of the two principles. This observation coupled with the above mentioned observation for random algorithms indicate that with  $T_u = 0.5$ , periodic update strategies perform as good as fresh information update strategies.

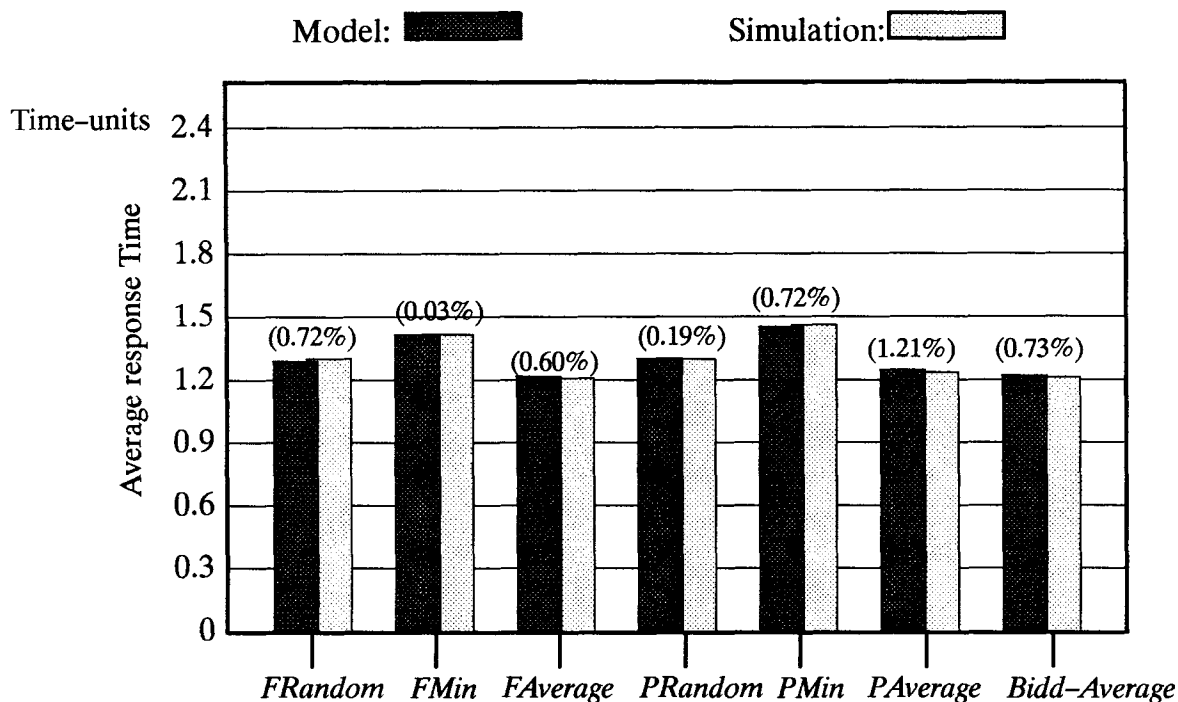


Figure 6: Comparison of response times predicted by the model and simulation for various strategies at low system load = 0.5,  $\mu_C = 16$  task/time-unit,  $\mu_S = 16$  task/time-unit,  $T_u = 0.5$  time-units and topology = 16 node hypercube

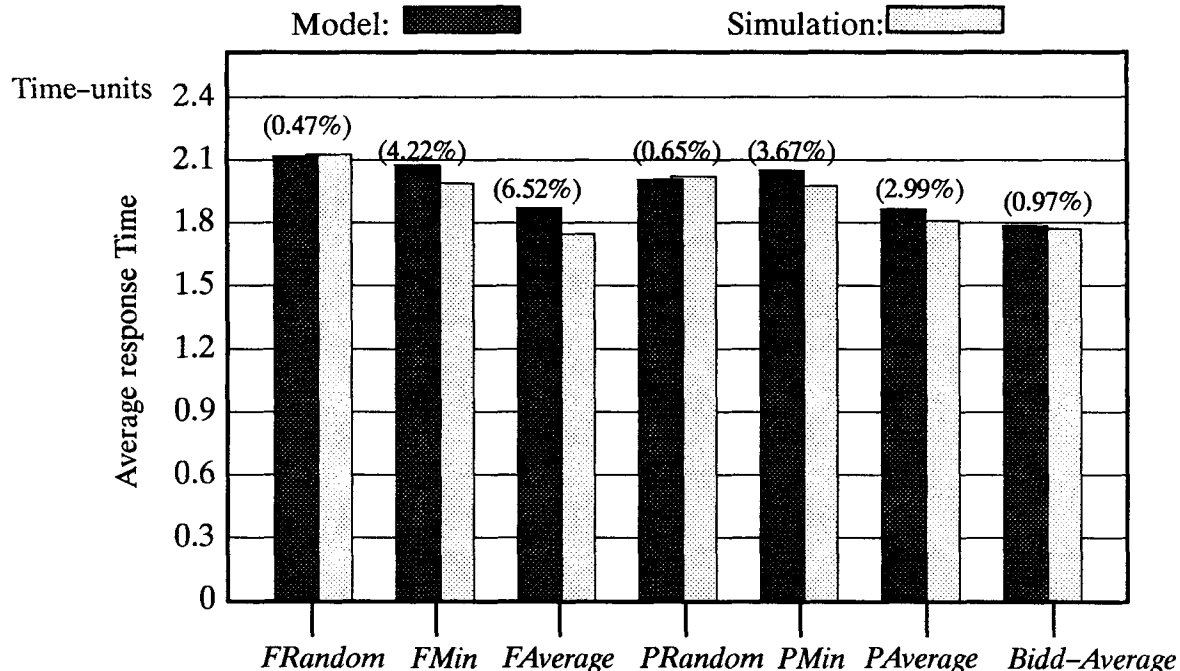


Figure 7: Comparison of response times predicted by the model and simulation for various strategies at high system load = 0.8,  $\mu_C = 16$  task/time-unit,  $\mu_S = 16$  task/time-unit,  $T_u = 0.5$  time-units and topology = 16 node hypercube

In order to check the validity of the proposed model for various parameters, we change  $\mu_S$  and  $\mu_C$  but keep the rest fixed. These results are shown in Figure 9 and Figure 10. A high system load, equal to 0.8, is selected by first considering a fast communication network and slow task scheduling rate ( $\mu_C = 16$  tasks/time-units and  $\mu_S = 16$  tasks/time-units), and then considering a slow network and fast task scheduling rate with ( $\mu_C = 8$  tasks/time-units and  $\mu_S = 16$  tasks/time-units). Again the model is shown to predict the average response time which closely matches the response time produced by simulation. Further insights drawn from these figures are summarized below.

- We note that task scheduling time has greater impact on the average task response time than the task communication time. This is obvious because the average response time with slow scheduling rate and high communication rate (Figure 8) is greater than the response time with fast scheduling rate and slow communication rate (Figure 9). The observation is true for all strategies. This should not be confused with the fact that  $P_0$  which was found insensitive to  $\mu_C$  for non-periodic load update strategies.  $P_0$  is only the probability with which a strategy schedules a task in local queue but  $\mu_C$  and  $\mu_S$  count towards queuing delays and service times at communications and input waiting queues, respectively.

Next, we show two arbitrarily chosen sets of system parameters. In the first set, a 16 node folded hypercube with 5 links per node at relatively low system load (0.6) is selected. The task communication rate and the task scheduling rate are both 12 tasks/time-unit and  $T_u$  is equal to 1.5 time-unit which is relatively large. The results for this combination of parameters are shown in Figure 10 and are summerized below.

- The difference in the response time for the model and simulation is again very small.
- The periodic update strategies, PMin and PAverage, are outperformed by FMin and FAverage because of the larger value of  $T_u$ .
- On the other hand, FRandom and PRandom yield identical results by showing their insensitivity to the load update method.

In the second set, we have selected a 16 node ring network with medium system load equal 0.7. Again, the response times predicted by the model match those produced by the simulation, as shown in Figure 11.

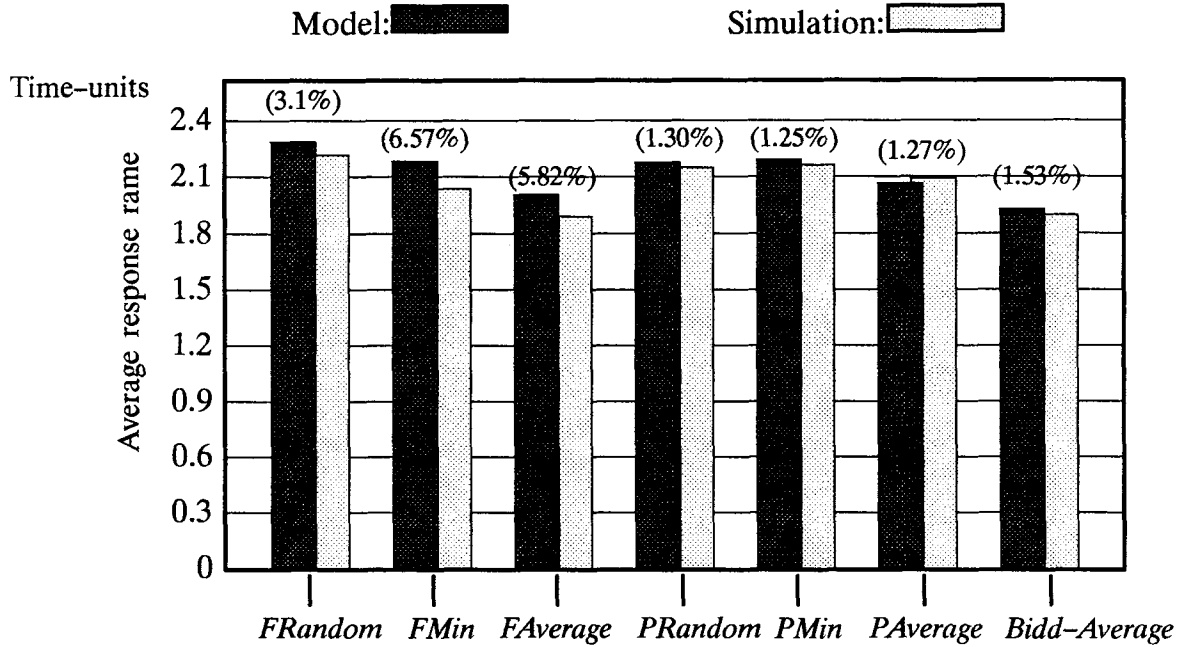


Figure 8: Comparison of response times predicted by simulation and the model for various strategies at high system load = 0.8 with fast communication,  $\mu_C = 16$  task/time-unit, high scheduling overhead (low rate),  $\mu_S = 8$  task/time-unit,  $T_u = 1.0$  time-units and topology = 16 node hypercube

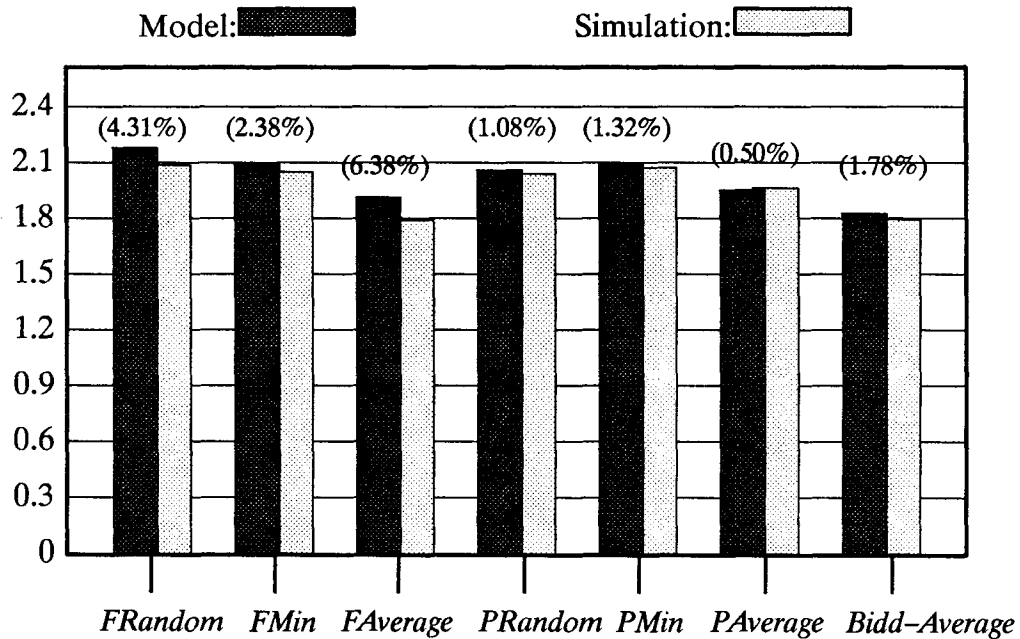


Figure 9: Comparison of response times predicted by simulation and the model for various strategies at high system load = 0.8 with slow communication,  $\mu_C = 8$  task/time-unit, low scheduling overhead (high rate),  $\mu_S = 16$  task/time-unit,  $T_u = 1.0$  time-units and topology = 16 node hypercube

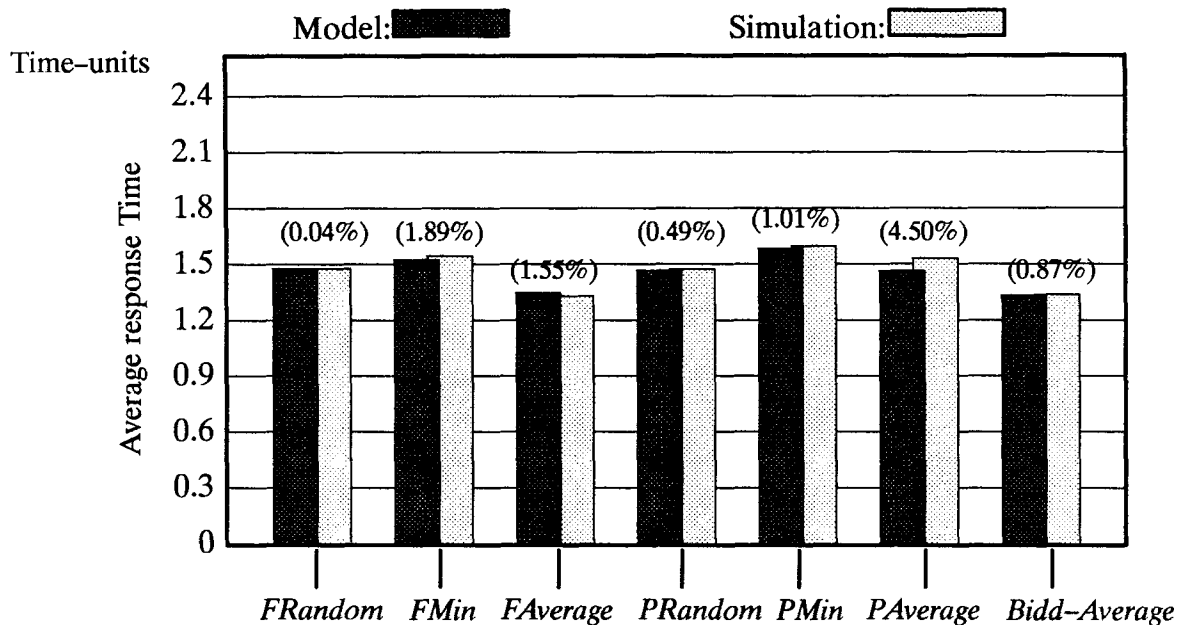


Figure 10: Comparison of response times predicted by the model and simulation for various strategies at medium system load,  $\lambda = 0.6$  task/time-unit and large load update period  $T_u = 1.5$  time-units, for 16 node Folded Hypercube with  $\mu_C = 12$  task/time-unit and  $\mu_S = 12$  task/time-unit

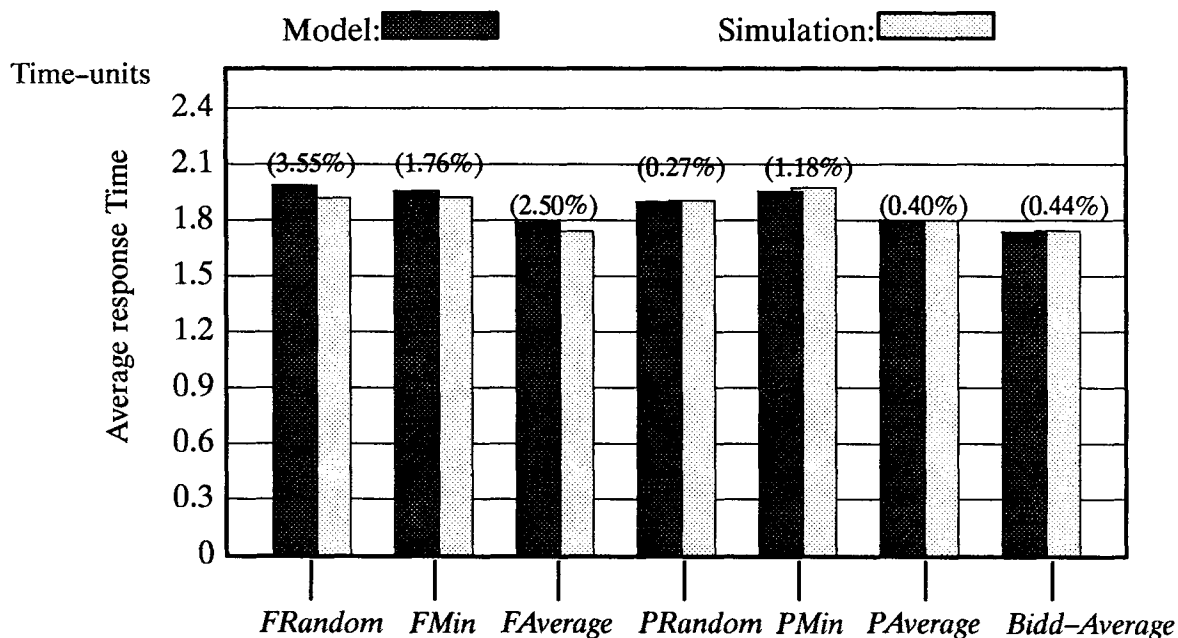


Figure 11: Comparison of response times predicted by the model and simulation for various strategies at system load,  $\lambda = 0.7$  task/time-unit and load update period  $T_u = 1.0$  time-units for 16 node ring with  $\mu_C = 12$  task/time-unit and  $\mu_S = 12$  task/time-unit



Up to this point, the performance of the model is compared with the same simulation test cases through which empirical data for statistical modeling was obtained. After characterizing  $P_0$  and  $E[N_E]$ , the queueing model was used to compute the average response time and the results were compared with the same simulation results. Therefore the comparison of the model with simulation has only revealed the correctness of the model. The validity of the proposed model is more strongly established as we obtain response time from the model and compare it with some additional simulation runs. The empirical data from these simulation runs has not been used for statistical modeling. The additional simulation runs include different network topologies with different parameters. The results of some combinations are shown in Figure 12, 13 and 14. By examining these figures, we conclude the following.

- Again, the difference between any pair of data sets does not exceed  $\pm 7\%$ .
- *Bidd-Average* performs consistently better than all other schemes and *Faverage* performs almost equally good.
- *PAverage* performs as good as *FAverage*, given that  $T_u$  is small.
- All nearest neighbor load balancing strategies perform better if the number of links per node are increased. This is because the probability that a node finds a suitable neighbor for task migration improves with increase in the number of links.
- The difference in the performance of ‘random’ strategies and ‘min’ strategies is not very significant as compared to the difference in the performance of ‘random’ and ‘averaging’ strategies.
- Random algorithms can be used with periodic information update for any network topology because periodic information update generates less message traffic. This is especially true for the fully connected network where *PRandom* performs as good as *FRandom*.
- If the actual scheduling time,  $1/\mu_s$ , for the random algorithm is less than that for ‘min’ algorithms, then *PRandom* can be used instead of *FMin*, *PMin* or *FRandom*.
- If the actual scheduling time,  $1/\mu_s$ , for ‘averaging’ algorithms is less than *Bidd-Averaging*, *PAveraging* should be used for network topologies such as ring or chordal ring and *FAverage* should be used for more dense [9] network topologies such as the fully connected network.

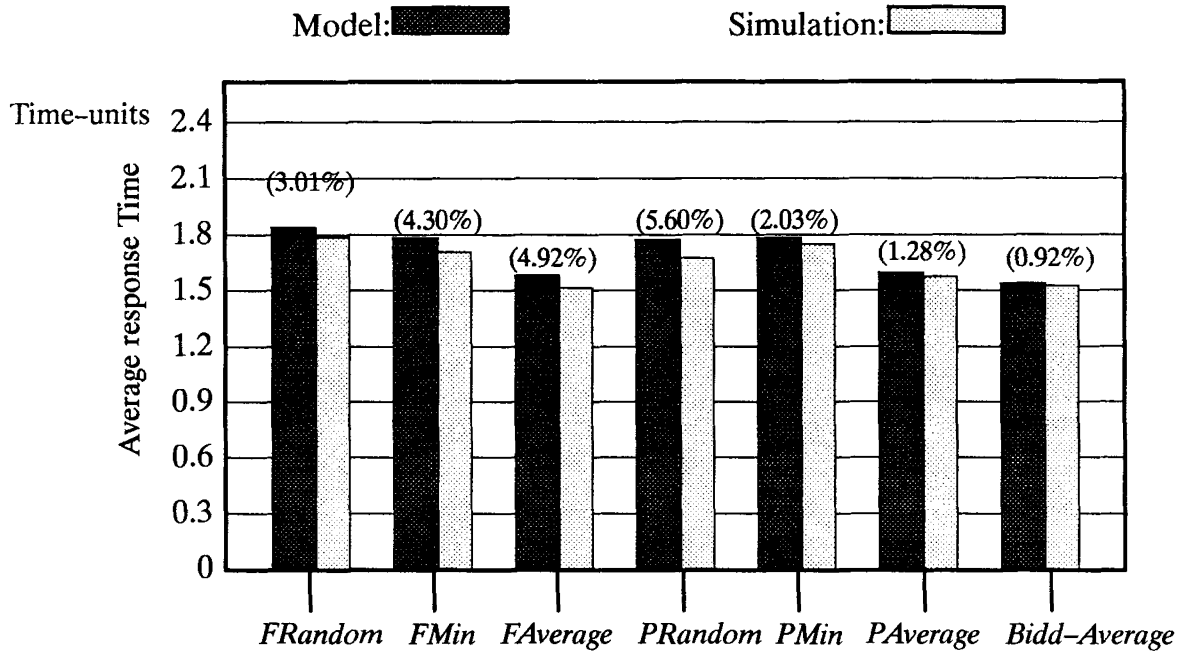


Figure 12: Comparison of response times predicted by the model and simulation for various strategies at system load,  $\lambda = 0.7$  task/time-unit and load update period  $T_u = 1.0$  time-units for 9 node mesh network with  $\mu_C = 16$  task/time-unit and  $\mu_S = 16$  task/time-unit

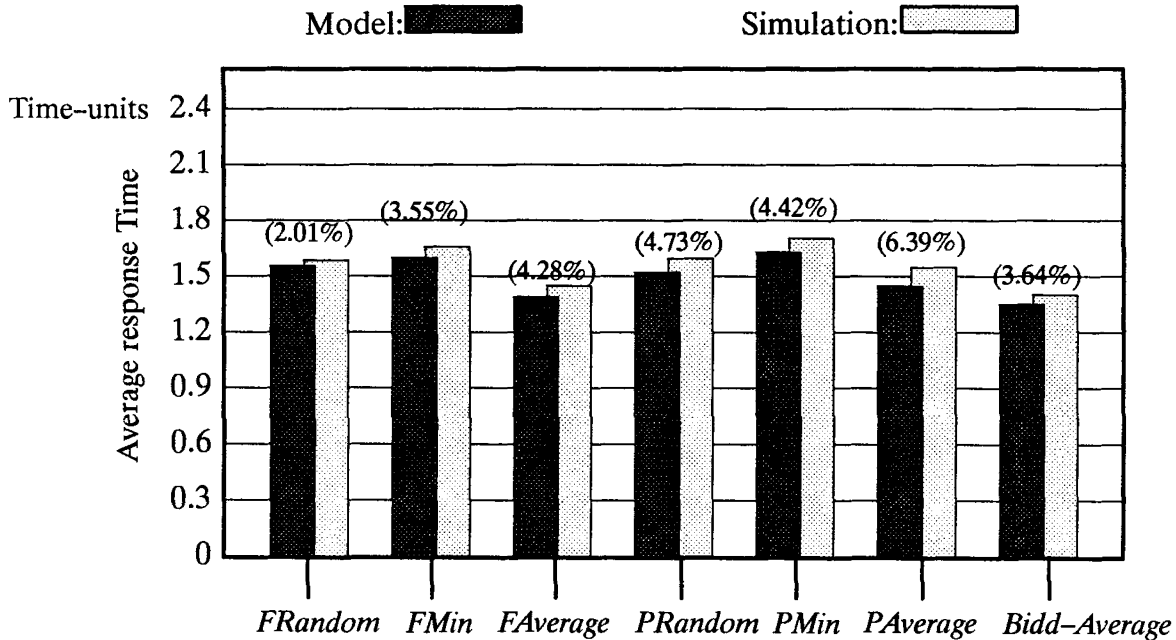


Figure 13: Comparison of response times predicted by the model and simulation for various strategies at system load,  $\lambda = 0.7$  task/time-unit and load update period  $T_u = 1.0$  time-units for 8 node fully connected network with  $\mu_C = 16$  task/time-unit and  $\mu_S = 16$  task/time-unit

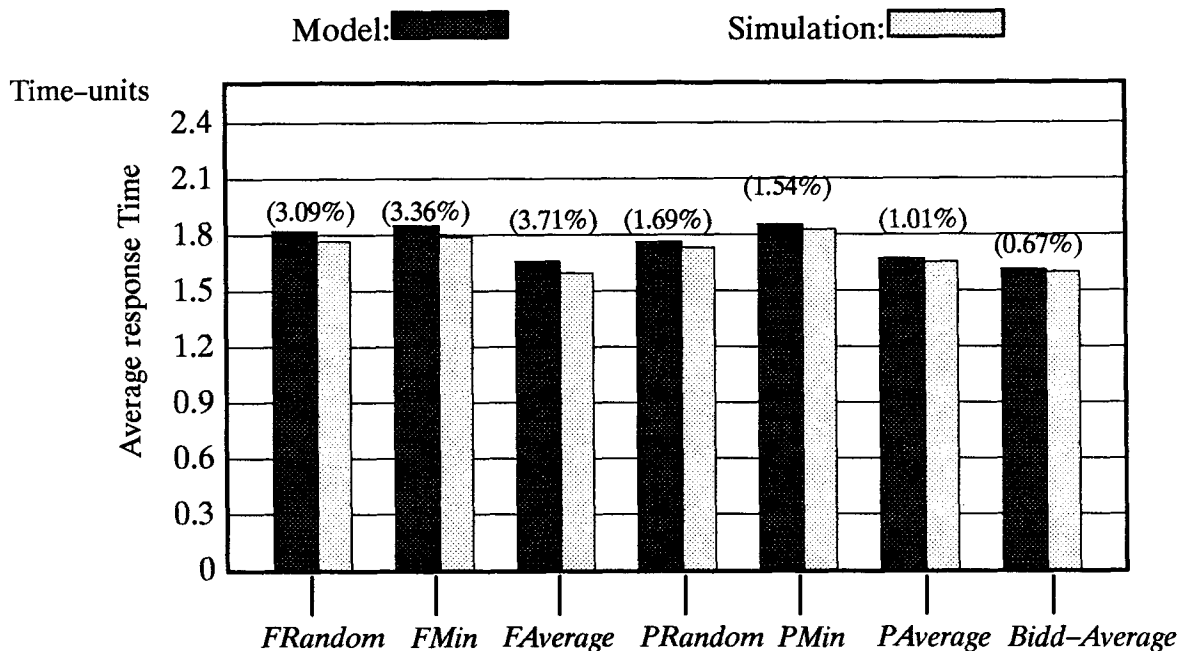


Figure 14: Comparison of response times predicted by the model and simulation for various strategies at system load,  $\lambda = 0.7$  task/time-unit and load update period  $T_u = 1.0$  time-units for 6 node chordal ring network with  $\mu_C = 16$  task/time-unit and  $\mu_S = 16$  task/time-unit

## 5. Summary

In this paper, we have presented an approach for modeling the average task response time for distributed load balancing in multicomputer systems. With this approach, we are able to compare different load balancing schemes on a unified basis. The class of load balancing strategies examined belong to the sender-initiated class. We have shown that these strategies can be modeled by an open central server queuing network if the system is symmetric and homogeneous. We believe that any sender-initiated load balancing strategy can be modeled by this queuing network. We have shown that for this model, we need to know only  $P_0$  and  $E[N_E]$ . The statistical characteristics of seven load balancing strategies are presented by showing the sensitivity of their queuing parameters with respect to various system parameters. By considering examples from a wide range of system parameters, it is shown that the average task response time predicted through the proposed model closely matches the response time obtained via simulation. The proposed performance prediction approach can be useful for analyzing and tuning an existing system, and evaluating newly proposed strategies. This approach can also be useful to select a suitable scheme for a given system.

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